

2.2 Part 2 Problem-Solving Strategy: Working Backwards

There are several strategies for solving problems:

- work backwards
- make a table
- guess & check
- act it out
- solve a simpler problem
- look for a pattern
- make a diagram
- eliminate possibilities

1. An ice sculpture is melting at a rate of half its weight every hour. After 8 hours, it weighs $\frac{5}{16}$ of a pound. How much did it weigh in the beginning?

$$\frac{5}{16} \times 2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 2$$

$$\boxed{80 \text{ lb}}$$

every hour mult. by $\frac{1}{2}$ → div by $\frac{1}{2}$
 mult. by rec
 mult by 2

2. A number is ^{add 35} decreased by 35, then ^{divide by 6} multiplied by 6, then ^{subtract 87} added to 87, then ^{mult. by 3} divided by 3. The result is 67.
What is the number?

$$\begin{array}{r}
 67 \times 3 = 201 \\
 - 87 \\
 \hline
 114 \div 6 = 19 \\
 + 35 \\
 \hline
 \boxed{54}
 \end{array}$$

3. Kristin spent one fifth of her money for gas. Then she ^{divide by 1/2 / mult. by 2} spent half of what was left for a haircut. She bought lunch for \$7. When she got home, she had \$13 left. How much did Kristin have originally?

$$\begin{array}{r}
 13 \\
 + 7 \\
 \hline
 20 \times 2 = 40 \cdot \frac{5}{4} = \boxed{\$50}
 \end{array}$$

^{4/5 of her money}
 ↓

4. The price of a television at Walmart is now two-thirds of the price it was last week. ^{mult by $\frac{3}{2}$} Now the price is $\$360$. What was the price last week?

$$360 \cdot \frac{3}{2} = \$540$$

5. Each year a particular car is worth about five-sevenths of its value the previous year. ^{mult by $\frac{7}{5}$} Now this car is worth $\$12,000$. What was its value two years ago?

$$12,000 \cdot \frac{7}{5} \cdot \frac{7}{5} = \$23,520$$

1. A number is doubled. Then 5 is subtracted from the result and the new result is divided by 3. The final result is 25.

What is the number?

$$\begin{array}{r} 25 \times 3 = 75 \\ + 5 \\ \hline 80 \div 2 = \boxed{40} \end{array}$$

2. A number is increased by 25. Then the result is multiplied by 2 and 27 is subtracted from the new result. The final result is 223.

What is the number?

$$\begin{array}{r} 223 \\ + 27 \\ \hline 250 \div 2 = 125 \\ - 25 \\ \hline \boxed{100} \end{array}$$

3. The price on a camera is now four-fifths of the price it was two weeks ago. Now the price is \$250. What was the price two weeks ago?

$$\$ 250 \cdot \frac{5}{4} = \frac{625}{2} = \$312.50$$

4. An icicle is melting at the rate of three-fourths of its weight every hour. After 3 hours, it weighs five-eighths of a pound. How much did it weigh in the beginning?

$$\frac{5}{8} \cdot \frac{4}{3} \cdot \frac{4}{3} \cdot \frac{4}{3} = \boxed{\frac{40}{27} \text{ lb}}$$

5. Each year a computer part is worth about two thirds of its value the previous year.

Now this part is worth \$60. What was its value two years ago?

$$\$60 \cdot \frac{3}{2} \cdot \frac{3}{2} = \$135$$