

2.7 A PREVIEW OF TRANSFORMATIONS

3 Types of Transformations

1. **Translation:** moving the graph up, down, left or right
2. **Stretch or Compression:** stretching or "squishing" the graph
3. **Reflection:** reflecting the graph across an axis

HIOVOS: A trick for remembering

Horizontal

Inside

Opposite

Vertical

Outside

Same

If you see...

Then it means...

Addition or
Subtraction

Translation

Horizontal: "inside" the function/OPPOSITE (left or right)
Vertical: "outside" the function/SAME (up or down)

Multiplication
(Integers &
Fractions)

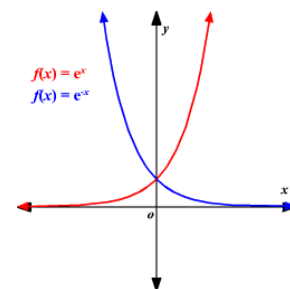
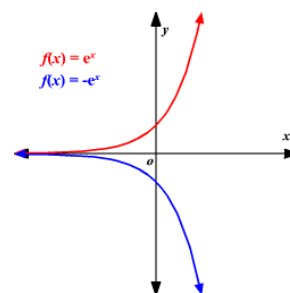
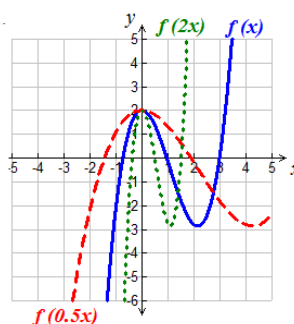
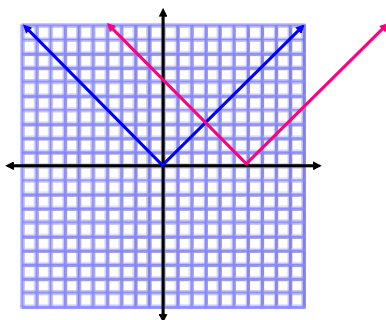
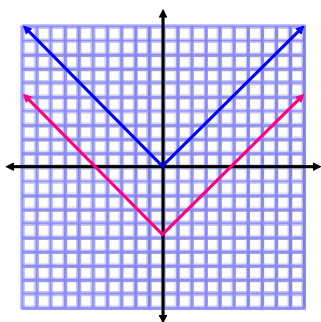
Stretch or Compression

Horizontal: "inside" the function/OPPOSITE (reciprocal) Vertical: "outside" the function/SAME
State the factor by which the graph is stretched (greater than 1) or compressed (greater than zero/less than 1)

Negative Sign

Reflection

Horizontal: "inside" the function (over y-axis)
Vertical: "outside" the function (over x-axis)



TRANSLATION

Original: $y = x^2$

Inside: $y = (x + 2)^2$ hor. translation left 2 units

$y = (x - 2)^2$ hor. translation right 2 units

Outside: $y = x^2 + 2$ vert. translation up 2 units

$y = x^2 - 2$ vert. translation down 2 units

STRETCH/COMPRESSION

Original: $y = x^2$

Inside: $y = (2x)^2$ hor. compression by a factor of $\frac{1}{2}$

$y = (\frac{1}{2}x)^2$ hor. stretch by a factor 2

Outside: $y = 2x^2$ vert. stretch by a factor of 2

$y = \frac{1}{2}x^2$ vert. compression by a factor of $\frac{1}{2}$

REFLECTION

Original: $y = x^2$

Inside: $y = (-x)^2$ hor. reflection over y-axis

Outside: $y = -x^2$ vert. reflection over x-axis

Describe the transformations of each from $y = |x|$.

1. $y = 4|x|$ vertical stretch by a factor of 4

2. $y = |4x|$ hor. compression by a factor of $\frac{1}{4}$

3. $y = -|x|$ vert. reflection over x-axis

4. $y = \frac{1}{3}|x - 2|$ hor. stretch by a factor of 3
vert. translation down 2 units

5. $y = |x - 2|$ hor. translation 2 units right

6. $y = -5|x + 2|$ vert. reflection over x-axis
hor. compression by a factor of $\frac{1}{5}$
vert. translation up 2 units

7. $y = \frac{1}{2}|x - 1|$ vertical compression by a factor of $\frac{1}{2}$
vert. translation down 1 unit

8. $y = -2|x - 4| + 5$ vert. reflection over x-axis
vert. stretch by a factor of 2
hor. translation right 4 units
vert. translation up 5 units

Write an equation of the transformed function described below in each problem.

9. $[x]$ **Step Function:** Vertical shift up 3 units ^{+3 outside}, Horizontal shift to the left 2 units ^{inside +2}, Vertical compression by a factor of $\frac{1}{2}$ ^{mult. by $\frac{1}{2}$}

$$y = \frac{1}{2} [x + 2] + 3$$

10. $|x|$ **Absolute Value:** Vertical shift down 4 units ^{outside -4}, Reflection over the x-axis ^{outside -}, Horizontal compression by a factor of $\frac{1}{2}$ ^{inside mult. by 2}

$$y = -|2x| - 4$$

11. $[]$ **Step Function:** Vertical shift up 1 unit ^{outside +1}, Horizontal shift to the right 5 units ^{inside -5}, Vertical stretch by a factor of 2 ^{outside mult. by 2}

$$y = 2 [x - 5] + 1$$

Graph each function. Find the domain and range.

13. $y = 1 \left[\frac{1}{2}x \right] - 5$
 Step function
 hor. stretch by a factor of 2
 vert. trans. 5 units down

