

8.7 PART 1 **FACTORIZING DIFFERENCES OF SQUARES**

Remember this pattern from earlier in the chapter?

DIFFERENCE OF SQUARES

$$a^2 - b^2 = (a + b)(a - b)$$

EXAMPLE:  $9x^2 - 25$ 

$$\begin{array}{c} \downarrow \quad \downarrow \\ (3x)^2 - (5)^2 \\ \text{"a"} \quad \text{"b"} \\ (3x + 5)(3x - 5) \end{array}$$

**EXAMPLES:** **FACTOR EACH BINOMIAL, IF POSSIBLE.**

$$\begin{array}{l} 1. \quad \overset{\checkmark}{m}^2 - \overset{\checkmark}{81} \\ \quad \quad (\overset{\checkmark}{m})^2 - (\overset{\checkmark}{9})^2 \\ \quad \quad (m+9)(m-9) \end{array}$$

$$\begin{array}{l} 2. \quad \overset{\checkmark}{25}t^2 - \overset{\checkmark}{6} \\ \quad \quad (\overset{\checkmark}{5t})^2 - (\quad)^2 \\ \quad \quad \text{prime} \end{array}$$

$$\begin{array}{l} 3. \quad \overset{\times}{8}y^2 - \overset{\checkmark}{1} \\ \quad \quad (\quad)^2 \\ \quad \quad \text{prime} \end{array}$$

$$\begin{array}{l} 4. \quad \overset{\checkmark}{9}h^2 - \overset{\checkmark}{64} \\ \quad \quad (\overset{\checkmark}{3h})^2 - (\overset{\checkmark}{8})^2 \\ \quad \quad (3h+8)(3h-8) \end{array}$$

**EXAMPLES:** FACTOR EACH BINOMIAL, IF POSSIBLE.

$$5. \quad \sqrt{9x^2} - \sqrt{100y^4}$$

$$\quad \quad (3x)^2 \quad (10y^2)^2$$

$$(3x - 10y^2)(3x + 10y^2)$$

$$6. \quad \sqrt{\frac{1}{9}g^2} - \sqrt{\frac{4}{25}}$$

$$\quad \quad \left(\frac{1}{3}g\right)^2 \quad \left(\frac{2}{5}\right)^2$$

$$\left(\frac{1}{3}g + \frac{2}{5}\right)\left(\frac{1}{3}g - \frac{2}{5}\right)$$

$$7. \quad \sqrt{49w^2} - \sqrt{16}$$

$$\quad \quad (7w)^2 \quad (4)^2$$

$$(7w - 4)(7w + 4)$$

$$8. \quad \sqrt{\frac{49}{16}c^4} - \sqrt{\frac{81}{100}d^2}$$

$$\quad \quad \left(\frac{7}{4}c^2\right)^2 \quad \left(\frac{9}{10}d\right)^2$$

$$\left(\frac{7}{4}c^2 - \frac{9}{10}d\right)\left(\frac{7}{4}c^2 + \frac{9}{10}d\right)$$

ALWAYS  
LOOK  
FOR A  
GCF  
FIRST!!

$$9. \quad 50 - 98d^2 = 0$$

$$2(\sqrt{25} - \sqrt{49d^2}) = 0$$

$$\downarrow \quad (5)^2 \quad (7d)^2 \quad \downarrow$$

$$2(5 - 7d)(5 + 7d) = 0$$

$$\begin{array}{r} 5 - 7d = 0 \\ -5 \\ \hline -7d = -5 \\ \frac{-7d}{-7} = \frac{-5}{-7} \\ \boxed{d = \frac{5}{7}} \end{array} \quad \begin{array}{r} 5 + 7d = 0 \\ -5 \\ \hline 7d = -5 \\ \frac{7d}{7} = \frac{-5}{7} \\ \boxed{d = -\frac{5}{7}} \end{array}$$

$$10. \quad 2c^2 - 32$$

$$2(\sqrt{c^2} - \sqrt{16})$$

$$\downarrow \quad (c)^2 \quad (4)^2$$

$$2(c - 4)(c + 4)$$

$$\begin{aligned}
 & \text{GCF} = 3x \\
 11. \quad & 75x^3 - 12xy^2 \\
 & 3x(25x^2 - 4y^2) \\
 & \quad \quad (5x)^2 \quad (2y)^2 \\
 & \quad \quad \downarrow \\
 & 3x(5x - 2y)(5x + 2y)
 \end{aligned}$$

$$12. \quad \frac{7}{4}n^2 - \frac{28}{9} = 0$$

$$7\left(\frac{1}{4}n^2 - \frac{4}{9}\right) = 0$$

$$\left(\frac{1}{2}n\right)^2 \quad \left(\frac{2}{3}\right)^2$$

$$7\left(\frac{1}{2}n - \frac{2}{3}\right)\left(\frac{1}{2}n + \frac{2}{3}\right) = 0$$

$$\frac{1}{2}n - \frac{2}{3} = 0$$

$$+\frac{2}{3} \quad +\frac{2}{3}$$

$$\frac{2}{1} \cdot \frac{1}{2}n = \frac{2}{3} \cdot \frac{2}{1}$$

$$n = \frac{4}{3}$$

$$\frac{1}{2}n + \frac{2}{3} = 0$$

$$-\frac{2}{3} \quad -\frac{2}{3}$$

$$\frac{2}{1} \cdot \frac{1}{2}n = -\frac{2}{3} \cdot \frac{2}{1}$$

$$n = -\frac{4}{3}$$

## CHALLENGE

$$13. \quad 32g^4 - 162h^4$$

$$2(16g^4 - 81h^4)$$

$$(4g^2)^2 \quad (9h^2)^2$$

$$2(4g^2 + 9h^2)(4g^2 - 9h^2)$$

$$(2g)^2 \quad (3h)^2$$

$$2(4g^2 + 9h^2)(2g + 3h)(2g - 3h)$$

$$14. \quad (c + d)^2 - e^2$$

$$(c + d + e)(c + d - e)$$