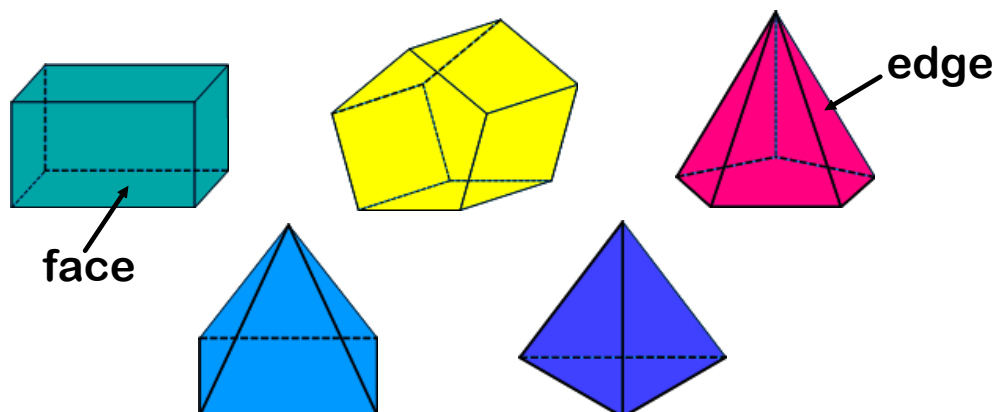
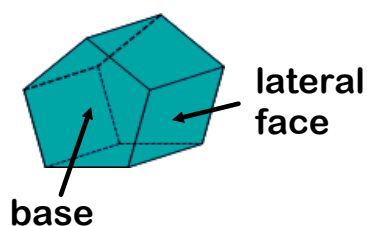


EXPLORING 3-DIMENSIONAL FIGURES

All of the surfaces of the solids so far are flat surfaces called **faces**. Solids with all flat surfaces that enclose a single region of space are called **polyhedrons** or **polyhedra**. All of the faces are polygons, and the line segments where the faces intersect are called **edges**.



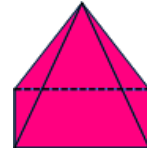
A **prism** is a polyhedron with two congruent faces that are polygons in parallel planes, that are called **bases**. The other faces, called **lateral faces**, are shaped like parallelograms.



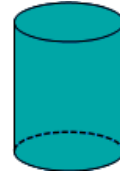
Prisms are named by the **shape of their bases**. The one above is a pentagonal prism.

A **regular prism** is a prism whose bases are regular polygons, such as in a **cube**.

A polyhedron that has all faces except one intersecting at one point is a **pyramid**.



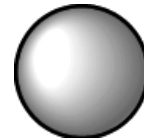
A **cylinder** is like a prism, but the bases are **circular**. This means that it is not a polyhedron.



A **cone** is like a pyramid, but the base is **circular**. It is also not a polyhedron.



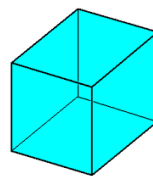
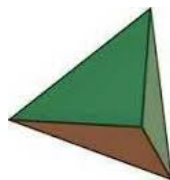
A **sphere** is a set of points in space that are a given distance from a given point.



A polyhedron is **regular** if all of its faces are shaped like congruent regular polygons.

There are exactly **five** types of regular polyhedra, and they are called **Platonic solids** because Plato described them so fully in his writings.

4 faces
tetrahedron

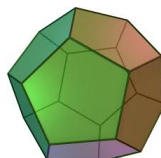


6 faces
hexahedron

8 faces
octahedron



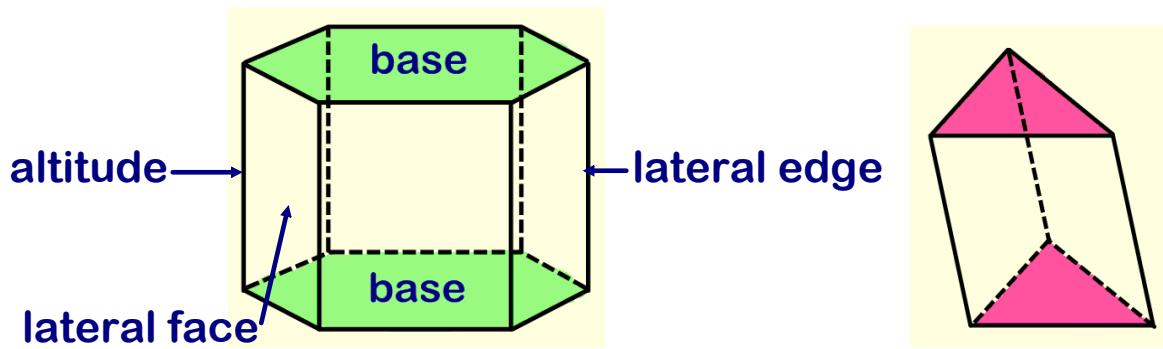
12 faces
dodecahedron



20 faces
icosahedron



SURFACE AREA OF PRISMS & CYLINDERS



A segment perpendicular to the planes containing the two bases, with an endpoint in each plane, is called the **altitude**. The length of the altitude is called the **height**. A prism whose lateral edges are also altitudes is called a **right prism**. If a prism is not right, then it is an **oblique prism**.

surface area: the area of all the faces of a prism (includes bases)

Surface Area of a Right Prism

$T = Ph + 2B$ where T = total surface area

P = perimeter of base

h = height of **prism** (not height of base)

B = area of base

Example 1

Find the surface area of the rectangular prism.

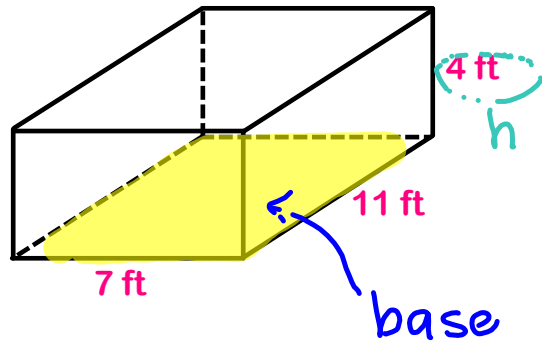
$$T = Ph + 2B$$

$$T = (36)(4) + 2(77)$$

$$T = 144 + 154$$

$$T = 298 \text{ ft}^2$$

dist.
b/w
bases



$$P = 7 + 11 + 7 + 11 = 36$$

$$h = 4$$

rect $A = lw$
or

$$B = 77$$

$$A = bh$$

$$A = 7 \cdot 11$$

Example 2

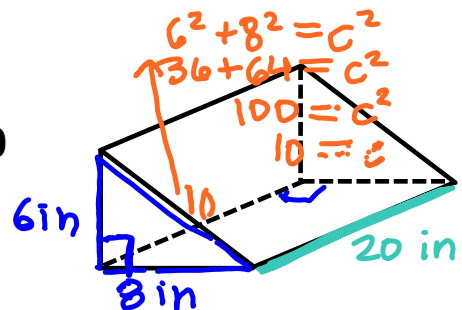
Find the surface area of a right triangular prism with a height of 20 inches and a right triangular base with legs of 8 and 6 inches.

$$T = Ph + 2B$$

$$T = (24)(20) + 2(24)$$

$$T = 480 + 48$$

$$T = 528 \text{ in}^2$$



$$P = 6 + 8 + 10 = 24$$

$$h = 20$$

$$B = 24$$

triangle

$$A = \frac{1}{2}bh$$

$$A = \frac{1}{2} \cdot 6 \cdot 8$$

$$A = 24$$

Example 3

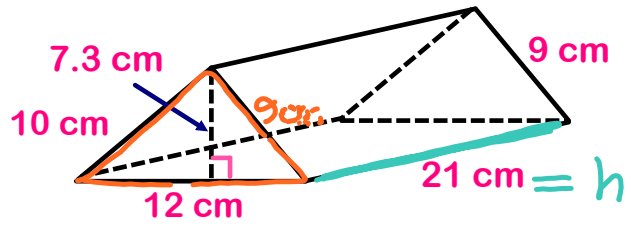
Find the surface area of the triangular prism.

$$T = Ph + 2B$$

$$T = (31)(21) + 2(43.8)$$

$$T = 651 + 87.6$$

$$T = 738.6 \text{ cm}^2$$



$$P = 10 + 12 + 9 = 31$$

$$h = 21$$

$$B = 43.8$$

triangle

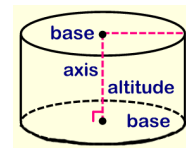
$$A = \frac{1}{2}bh$$

$$A = \frac{1}{2}(7.3)(12)$$

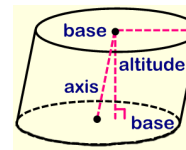
$$A = 43.8$$

A **cylinder** is like a prism but with circular bases. The **axis** of the cylinder is the segment whose endpoints are centers of the bases.

The **altitude** is a segment perpendicular to the planes containing the bases with an endpoint in each plane.



right cylinder



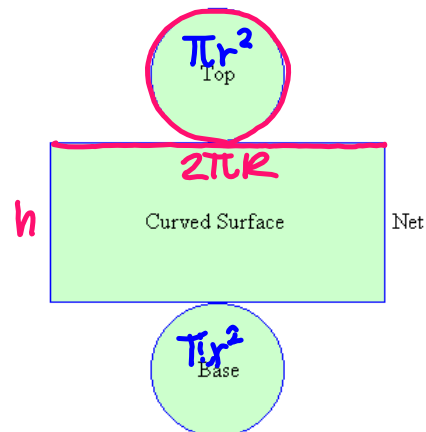
oblique cylinder

Surface Area of a Cylinder

$$T = 2\pi rh + 2\pi r^2$$

rectangle

2 circles



Example 4

Find the surface area of the right cylinder.

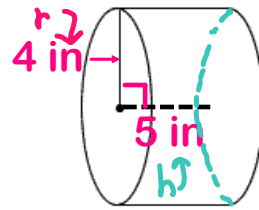
$$T = 2\pi rh + 2\pi r^2$$

$$T = 2\pi(4)(5) + 2\pi(4)^2$$

$$T = 40\pi + 32\pi$$

$$T = 72\pi$$

$$T \approx 226.2 \text{ in}^2$$

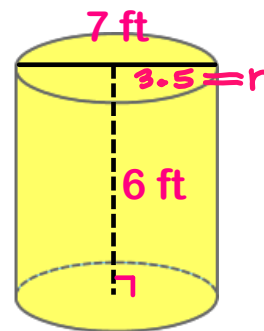
**Example 5**

Find the surface area of the right cylinder.

$$T = 2\pi rh + 2\pi r^2$$

$$T = 2\pi(3.5)(6) + 2\pi(3.5)^2$$

$$T \approx 208.9 \text{ ft}^2$$



Example 6

The surface area of a right cylinder is 200 square centimeters. If the diameter of the base is 10 $\rightarrow r = 5$ centimeters, find the height of the cylinder.

$$T = 2\pi r h + 2\pi r^2$$

$$200 = 2\pi(5)h + 2\pi(5)^2$$

$$200 = 10\pi h + 50\pi$$

$$\begin{array}{r} 200 - 50\pi = 10\pi h \\ \hline 10\pi \qquad \qquad 10\pi \end{array}$$

$$\boxed{1.4m \approx h}$$