

## 8.2 PART 2 MULTIPLYING POLYNOMIALS

### *Multiplying Binomials and Trinomials*

To multiply a binomial by a binomial, you can use the FOIL Method.  
 $(3x + 4)(x - 5)$

FIRST  
OUTER  
INNER  
LAST

$$(3x + 4)(x - 5)$$

$$\begin{aligned} & (3x)(x) + (3x)(-5) + (4)(x) + (4)(-5) \\ & 3x^2 \quad + \quad -15x \quad + \quad 4x \quad + \quad -20 \\ & \qquad\qquad\qquad \swarrow \quad \searrow \\ & 3x^2 \quad + \quad -11x \quad + \quad -20 \\ & \qquad\qquad\qquad \downarrow \\ & 3x^2 - 11x - 20 \end{aligned}$$

Use the FOIL method to find the product.

$$1. \quad (4x + 1)(2x - 3)$$

$$\begin{array}{r}
 \text{F} \quad (4x)(2x) + (4x)(-\overline{3}) + (\overline{1})(2x) + (\overline{1})(-\overline{3}) \\
 8x^2 \quad + \boxed{-} 12x \quad + \quad 2x \quad \boxed{+} \boxed{-} 3 \\
 8x^2 \quad \cancel{-} \underbrace{12x}_{\phantom{12x}} \quad + \underbrace{2x}_{\phantom{2x}} \quad - 3 \\
 8x^2 \quad - 10x \quad - 3
 \end{array}$$

Use the FOIL method to find the product.

$$2. \quad (x - 5)(6x - 7)$$

$$\begin{array}{r}
 \text{F} \quad (x)(6x) + (x)(-\overline{7}) + (-5)(6x) + (-5)(-\overline{7}) \\
 6x^2 \quad + \boxed{-} 7x \quad \boxed{+} \boxed{-} 30x \quad + \quad 35 \\
 6x^2 \quad \cancel{-} \underbrace{7x}_{\phantom{7x}} \quad \cancel{-} \underbrace{30x}_{\phantom{30x}} \quad + \quad 35 \\
 6x^2 \quad - 37x \quad + 35
 \end{array}$$

Use the FOIL method to find the product.

$$4. \quad (3x + 11)(4x + 7)$$

$$(3x)(4x) + (3x)(7) + (11)(4x) + (11)(7)$$

$$12x^2 + 21x + 44x + 77$$

$$12x^2 + 65x + 77$$

Use the FOIL method to find the product.

$$3. \quad (8x - 3)(2x + 1)$$

$$(8x)(2x) + (8x)(1) + (-3)(2x) + (-3)(1)$$

$$16x^2 + 8x + -6x + -3$$

$$16x^2 + \underbrace{8x - 6x}_{+ 2x} - 3$$

$$16x^2 + 2x - 3$$

You can also multiply  
two binomials  
using the  
distributive property.

Recall from Chapter 2,  
 $3(2x - 5)$  becomes  $6x - 15$ .

$$5. \quad x(3x^2 + 6x - 8)$$

$$6. \quad -3x(2x^2 - x + 4)$$

Use the distributive property to find the product.

$$(x + 2)(x - 3)$$

$$(x + 2)(x - 3)$$

$$x(x - 3) + 2(x - 3)$$

$$x(x) + x(-3) + 2(x) + 2(-3)$$

$$\begin{array}{r} x^2 \quad + \quad -3x \quad + \quad 2x \quad + \quad -6 \\ \qquad \qquad \searrow \quad \swarrow \\ x^2 \quad + \quad -1x \quad + \quad -6 \end{array}$$

$$x^2 - x - 6$$

Use the distributive property to multiply.

$$\begin{array}{l} 7. \quad \underline{(x - 2)}(\underline{x + 4}) \\ \quad \quad \quad x(x+4) \quad -2(x+4) \\ \quad \quad \quad x \cdot x + x \cdot 4 \quad -2 \cdot x \cancel{+} 2 \cdot 4 \\ \quad \quad \quad x^2 + 4x \quad \quad \quad -2x \quad - 8 \\ \quad \quad \quad x^2 + 2x \quad - 8 \end{array}$$

Use the distributive property to multiply.

8.  $(2x + 1)(x + 2)$

$$\begin{array}{r} 2x(x+2) \\ + 1(x+2) \end{array}$$

$$2x \cdot x + 2x \cdot 2 + 1 \cdot x + 1 \cdot 2$$

$$2x^2 + \underbrace{4x + x}_{\text{blue bracket}} + 2$$

$$2x^2 + 5x + 2$$

Regardless of whether you like the **FOIL** method or the **distributive property**... you MUST use the distributive property to multiply anything larger than binomials!

Use the distributive property to multiply.

9.  $(x + 4)(x^2 - 5x + 7)$

$$\begin{aligned}
 & (x + 4)(x^2 - 5x + 7) \\
 & x(x^2 - 5x + 7) + 4(x^2 - 5x + 7) \\
 & x \cdot x^2 - x \cdot 5x + x \cdot 7 + 4 \cdot x^2 - 4 \cdot 5x + 4 \cdot 7 \\
 & x^3 \boxed{-5x^2} \boxed{+7x} \boxed{+4x^2} \boxed{-20x} + 28 \\
 & x^3 - x^2 - 13x + 28
 \end{aligned}$$

Use the distributive property to multiply.

10.  $(x - 3)(3x^2 + x - 4)$

$$\begin{aligned}
 & x(3x^2 + x - 4) - 3(3x^2 + x - 4) \\
 & x \cdot 3x^2 + x \cdot x - x \cdot 4 - 3 \cdot 3x^2 \boxed{+ -3 \cdot x = -3 \cdot 4} \\
 & 3x^3 \boxed{+ x^2} \boxed{- 4x} \boxed{- 9x^2} \boxed{- 3x} + 12 \\
 & 3x^3 - 8x^2 - 7x + 12
 \end{aligned}$$