

5.5 Solving Absolute Value Equations

An absolute value equation is in the form $|ax + b| = c$.

To solve an absolute value equation when $c \geq 0$:

$$ax + b = c \quad \text{or} \quad ax + b = -c$$

Always isolate the absolute value before separating into two equations!!

Solve & graph the absolute value equations.

$$1. |x| = 7$$

distance = 7

$$x = -7 \text{ or } x = 7$$

$$2. |x| = 25$$

distance = 25

$$x = -25 \text{ or } x = 25$$

$$3. |x| = -4$$

distance = -4

no solution
(no neg. dist!)

Solve & graph the absolute value equations.

$$4. \left| \underline{x} - 2 \right| = 5$$

dist = 5

$$\begin{array}{l} x - 2 = -5 \text{ or } x - 2 = 5 \\ \cancel{+2} \quad \cancel{+2} \\ x = -3 \text{ or } x = 7 \end{array}$$

$$5. \left| x + 3 \right| = 18$$

dist = 18

$$\begin{array}{l} x + 3 = -18 \text{ or } x + 3 = 18 \\ \cancel{-3} \quad \cancel{-3} \\ x = -21 \text{ or } x = 15 \end{array}$$

Solve the absolute value equations.

$$6. \left| 4x + 6 \right| = 28$$

dist = 28

$$\begin{array}{l} 4x + 6 = -28 \text{ or } 4x + 6 = 28 \\ \cancel{-6} \quad \cancel{-6} \\ 4x = -34 \quad 4x = 22 \\ \frac{4x}{4} \quad \frac{4x}{4} \\ x = -\frac{17}{2} \quad x = \frac{11}{2} \end{array}$$

$$7. \left| 7 - 2x \right| = 19$$

dist = 19

$$\begin{array}{l} 7 - 2x = -19 \text{ or } 7 - 2x = 19 \\ \cancel{-7} \quad \cancel{-7} \\ -2x = -26 \quad -2x = 12 \\ \frac{-2x}{-2} \quad \frac{-2x}{-2} \\ x = 13 \quad x = -6 \end{array}$$

Solve the absolute value equations.

$$8. \frac{|x+1| + 2 = 5}{|x+1| = 3} \quad \text{dist=3}$$

$$\frac{x+1=-3}{x=-4} \quad \text{or} \quad \frac{x+1=3}{x=2}$$

$$9. \frac{|2x-8| - 14 = -4}{|2x-8| = 10} \quad \text{dist=10}$$

$$\begin{aligned} 2x-8 &= -10 & \text{or} & 2x-8 = 10 \\ +8 &+8 & & +8 &+8 \\ \frac{2x}{2} &= \frac{-2}{2} & & \frac{2x}{2} &= \frac{18}{2} \\ x &= -1 & & x &= 9 \end{aligned}$$

Solve the absolute value equations.

$$10. \frac{2|x-3|}{2} = \frac{16}{2} \quad |x-3| = 8 \quad \text{dist=8}$$

$$\frac{x-3=-8}{x=-5} \quad \text{or} \quad \frac{x-3=8}{x=11}$$

$$11. \frac{|x+4|}{5} = 3 \cdot 5 \quad |x+4| = 15 \quad \text{dist=15}$$

$$\frac{x+4=-15}{x=-19} \quad \text{or} \quad \frac{x+4=15}{x=11}$$