

4.2 Use Linear Equations in Slope-Intercept Form

Write an equation of the line in **slope-intercept form** that passes through the point $(-1, 3)$ and has a **slope of -4**.

$y = mx + b$
 x_1, y_1

$$\begin{aligned}
 y - y_1 &= m(x - x_1) \\
 y - 3 &= -4(x - (-1)) \\
 y - 3 &= -4x - 4 \\
 +3 & \qquad \qquad +3 \\
 \hline
 y &= -4x - 1
 \end{aligned}$$

Write an equation of the line in **slope-intercept form** that passes through the point $(6, 3)$ and has a **slope of -2**.

x_1, y_1

$$\begin{aligned}
 y - y_1 &= m(x - x_1) \\
 y - 3 &= -2(x - 6) \\
 y - 3 &= -2x + 12 \\
 +3 & \qquad \qquad +3 \\
 \hline
 y &= -2x + 15
 \end{aligned}$$

Write an equation of the line in **slope-intercept form** that passes through the point $(-3, -11)$ and has a **slope of $\frac{1}{2}$** .

$$y - y_1 = m(x - x_1)$$

$$y + 11 = \frac{1}{2}(x + 3)$$

$$y + 11 = \frac{1}{2}x + \frac{3}{2}$$

$$\begin{array}{r} y + 11 \\ -11 \\ \hline y = \frac{1}{2}x - \frac{19}{2} \end{array}$$

Write an equation of the line in **slope-intercept form** that passes through $(\frac{9}{2}, 1)$ and $(-\frac{7}{2}, 7)$.

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

$$m = \frac{7 - 1}{-\frac{7}{2} - \frac{9}{2}} = \frac{6}{-8} = -\frac{3}{4}$$

$$y - y_1 = m(x - x_1)$$

$$y - 1 = -\frac{3}{4}(x - \frac{9}{2})$$

$$y - 1 = -\frac{3}{4}x + \frac{27}{8}$$

$$\begin{array}{r} y - 1 \\ +1 \\ \hline y = -\frac{3}{4}x + \frac{35}{8} \end{array}$$

Your gym membership charges $\$35$ per month after an initial membership fee. Roger has paid a total of \$250 after 6 months.

- a) Write an equation that gives the total cost of a gym membership as a function of the length of membership.

$$\begin{aligned}
 y - y_1 &= m(x - x_1) \\
 y - 250 &= 35(x - 6) \\
 y - 250 &= 35x - 210 \\
 + 250 & \quad + 250 \\
 \hline
 y &= 35x + 40
 \end{aligned}$$

- b) Find the total cost of membership after 10 months.

$$\begin{aligned}
 y &= 35(10) + 40 \\
 y &= 350 + 40 \\
 y &= \$390
 \end{aligned}$$

A BMX race track charges a membership fee and an entry fee per race. Deandre paid a total of \$76 after 3 races. Chris paid a total of \$124 after 7 races.

- a) How much does the track membership cost?

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{124 - 76}{7 - 3} = \frac{48}{4} = 12$$

$$\begin{aligned}
 y - y_1 &= m(x - x_1) \\
 y - 76 &= 12(x - 3) \\
 y - 76 &= 12x - 36 \\
 + 76 & \quad + 76 \\
 \hline
 y &= 12x + 40
 \end{aligned}$$

- b) What is the entry fee per race?

\$12

- c) Write an equation that gives the total cost as a function of the number of races entered. $y = 12x + 40$